

# Residual lifetimes of consecutive $k$ -out-of- $n$ systems

Serkan Eryılmaz\*

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## Abstract

Consecutive type systems have attracted a lot of attention in the field of reliability. A linear consecutive  $k$ -out-of- $n$ :F (G) system consists of  $n$  linearly ordered components such that the system fails (functions) if and only if at least  $k$  consecutive components fail (function). These system models appear in various real life systems including telecommunication and oil pipeline systems, vacuum systems in accelerators, etc.

For some systems of order  $n$ , the system may still function with probability 1 when less than  $r(< n)$  components fail at time  $t$ . Let  $T$  denote the lifetime of a system whose components' lifetimes are  $T_1, T_2, \dots, T_n$ . If  $T_{r:n}$  denotes the  $r$ th smallest lifetime, then the conditional random variable  $\{T - t \mid T_{r:n} > t\}$  represents the general residual lifetime of the system under the condition that at least  $n - r + 1$  components of the system are working at time  $t$ . In this talk, we present some results on usual and general residual lifetimes of consecutive  $k$ -out-of- $n$  systems. Mean residual lifetimes of these systems are studied and a signature based analysis is also presented.

**Keywords.** Consecutive  $k$ -out-of- $n$  systems; Order statistics; Residual lifetime; System signature

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\*Izmir University of Economics, Department of Mathematics, 35330, Balçova, Izmir, Turkey  
e-mail: serkan.eryilmaz@ieu.edu.tr